

# Central bank digital currency in an open economy

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# Introduction

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- ✓ Several relevant *closed-economy* implications:
  - Equivalence result, [Brunnermeier & Niepelt \(2019\)](#)
  - Impact on banking sector, [Andolfatto \(2021\)](#)
  - Effects of different design alternatives & preferences, [Agur et al. \(2021\)](#) [Auer & Boehme \(2021\)](#)
  - Financial stability issues, [Fernández-Villaverde et al. \(2020\)](#)
  - Technical literature on design, [Bindseil & Panetta \(2020\)](#)

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- ✓ We build a two-country macro model drawing from Eichenbaum et al (2021) and add a CBDC to the menu of monetary assets
- ✓ CBDC choice is micro-founded in three dimensions: *preferences*, *liquidity*, *remuneration*
- ✓ Main findings:
  - Derive a new cross-country parity condition between interest rates, CBDC remuneration & exchange rates
  - CBDC amplifies international spillovers of shocks
  - Design features matter
  - CBDC reduces monetary policy autonomy in foreign economies

# The model

## a. Preferences: augmented utility function

Household choose consumption ( $C$ ), labor ( $L$ ), M1 money ( $M$ ), bond holdings ( $B, B^*$ ), deposits ( $D$ ) and CBDC ( $DC$ ).

Intra-period utility is:

$$U_t = \exp(e_t^C) \ln(C_t - hC_{t-1}) - \frac{\chi}{1+\varphi} L_t^{1+\varphi} - \overbrace{\chi_{DC} \mathcal{G}\left(\frac{M_t}{M_t + DC_t}, \Gamma\right)}^{\text{Preferences over payment instruments}}$$

with  $\exp(e_t^C)$  a preference shock

## a. Preferences: augmented utility function

$$U_t = \exp(e_t^C) \ln(C_t - hC_{t-1}) - \frac{\chi}{1+\varphi} L_t^{1+\varphi} - \chi_{DC} \mathcal{G}\left(\frac{M_t}{M_t + DC_t}, \Gamma\right)$$

- ✓  $\chi_{DC}$  scale parameter
- ✓  $\frac{M_t}{M_t + DC_t}$  optimal cash/CBDC ratio **chosen** by households
- ✓  $\Gamma$  **preferred** cash/CBDC ratio by households; this is driven by preferences over anonymity, payment habits and other tastes

## a. Preferences: augmented utility function

$$U_t = \exp(e_t^C) \ln(C_t - hC_{t-1}) - \frac{\chi}{1+\varphi} L_t^{1+\varphi} - \chi_{DC} \mathcal{G} \left( \frac{M_t}{M_t + DC_t}, \Gamma \right)$$

→  $\mathcal{G}(\bullet)$  **utility loss** if  $\Gamma \neq \frac{M_t}{M_t + DC_t}$

✓  $\mathcal{G}(0) = 0$ , global minimum for  $\frac{M_t}{M_t + DC_t} = \Gamma$

✓  $\mathcal{G}'(x_0)$  exists  $\forall x_0 \in \mathbb{R}$  (differentiability)

✓  $\mathcal{G}(\bullet)' > 0$ ,  $\mathcal{G}(\bullet)'' < 0$ , (concavity)

→ **Intuition:** households have different members, some prefer paying with cash, the others with CBDC



## b. Liquidity: CIA constraint

Households need liquidity to consume:

$$C_t = \mathcal{L}_t(M_t, DC_t)$$

- $\mathcal{L}(\bullet)$  liquidity aggregator of cash and CBDC
  - ✓ in baseline  $\mathcal{L}'_{M_t}(x_0) = \mathcal{L}'_{DC_t}(x_0)$  (same marginal liquidity)
  - ✓ in extensions  $\mathcal{L}'_{M_t}(x_0) > \mathcal{L}'_{DC_t}(x_0)$ ;  $\mathcal{L}'_{M_t}(x_0) < \mathcal{L}'_{DC_t}(x_0)$
  
- **Intuition:** households need liquidity services to make transactions, CBDC and cash are (imperfect) substitutes

## c. Remuneration: budget constraint

Households balance returns across all asset classes to smooth consumption across periods:

$$\begin{aligned}
 P_t C_t + B_t^H + NER_t B_t^F + D_t + M_t + DC_t \leq & W_t L_t + \\
 + R_t B_{t-1}^H + R_t^* NER_t B_{t-1}^F - \frac{\phi^B}{2} \left( \frac{NER_t B_t^F}{P_t} \right)^2 & P_t + \\
 + D_{t-1} R_t^D + \zeta^\$ M_{t-1} + R_t^{DC} DC_{t-1} + \Pi_t &
 \end{aligned}$$

- households balance returns on cash, bonds (domestic and foreign) deposits and CBDC
- $\zeta^\$$  storage cost for cash (= 1 in baseline)
- $R^{DC} = 1$  in baseline (no remuneration on CBDC)
- $\phi^B > 0$  cross-country bond holding costs (imperfect risk-sharing, UIP fails)

# Optimal CBDC demand

Preferences, liquidity, remuneration (relative to other assets) all matter:

$$\underbrace{\mathcal{L}'_{DC,t} \gamma_t}_{\text{Value of liquidity services}} - \underbrace{\chi_{DC} \mathcal{G}'_{DC,t}}_{\text{Utility loss}} = \lambda_t - E_t \left( \overbrace{\left( \beta R_t^{DC} \frac{\lambda_{t+1}}{\pi_{t+1}} \right)}^{\text{Expected returns}} \right)$$

## Similar setting with key differences

- ✓ No CBDC in the foreign country, foreign household can buy the CBDC issued in the domestic country
- ✓ Exchange rate value effects matter when choosing CBDC demand in the foreign economy
- ✓ There are costs ( $\approx$  transaction limits) in cross-border CBDC transactions ( $\phi_{DC}^*(DC_t^*, NER_t)$ )

# Optimality condition

$$\underbrace{\mathcal{L}_{DC,t}^{*,\prime} \gamma_t^*}_{\text{Value of liquidity services}} - \underbrace{\chi_{DC}^* \mathcal{G}_{DC,t}^{*,\prime}}_{\text{Utility loss}} =$$

$$\underbrace{\lambda_t^* \phi_{DC}^{*,\prime} (DC_t^*, NER_t)}_{\text{Limits to cross-border transactions}} + \frac{\lambda_t^*}{NER_t} - E_t \left( \underbrace{\beta^* \frac{\lambda_{t+1}^*}{NER_{t+1}} \frac{R_t^{DC}}{\pi_{t+1}^*}}_{\text{Expected returns}} \right)$$

## The key mechanism

Combining CBDC and bond demands in the foreign economy leads to a (linearized) new UIP condition:

$$r_t^* = r_t^{DC} + ner_t - E_t ner_{t+1} + m_t$$

where  $m_t$  is a **mark-up** depending on liquidity services ( $\uparrow$ ), preferences for cash ( $\downarrow$ ) and cross-border costs ( $\downarrow$ ).  $r_t^{DC} = 0 \forall t$  (CBDC not remunerated in baseline).

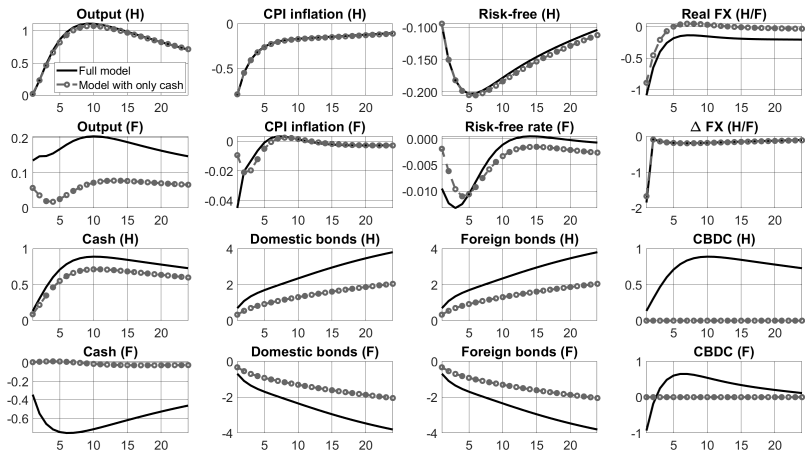
### Implications:

- if  $E_t ner_{t+1} > 0$ ,  $ner_t < 0$  (stronger FX overshooting)
- if  $E_t ner_{t+1} > 0$ ,  $r_t^* < 0$  (stronger policy response)
- if  $r_t^{DC} \neq 0$ , above effects should be smaller

Derivations. Comparison with standard UIP.

# Results

# TFP shock in the domestic economy

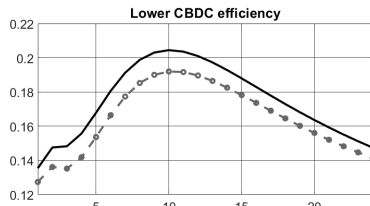
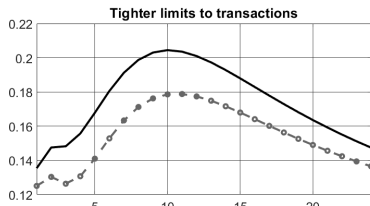
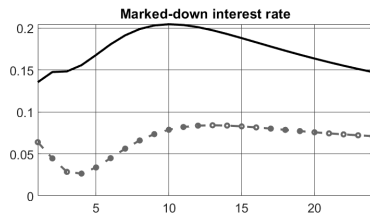
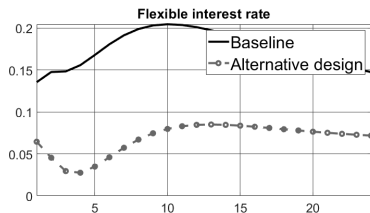


**Figure:** Response of selected variables to a one standard deviation expansionary total factor productivity shock in the domestic economy. Solid lines refer to the baseline calibration with a CBDC, dashed lines with circles to a simulation without a CBDC.

**Notes:** Responses are reported in deviations from the steady state.



# Alternative design choices



**Figure:** Response of foreign output to a one standard deviation expansionary total factor productivity shock in the domestic economy under alternative CBDC designs.

**Notes:** Responses are reported in deviations from the steady state.

# Optimal monetary policy with and without CBDC

	No CBDC	Fixed interest rate	Flexible interest rate	Marked-down interest rate
Domestic economy				
$\gamma$	0.001	0.001	0.001	0.001
$\theta_\pi$	3.57	4.00	3.60	4.00
$\theta_y$	0.00	0.17	0.00	0.00
$\Delta E(\mathcal{W})$	0.00	7.40	1.02	1.21
Foreign economy				
$\gamma^*$	0.823	0.827	0.832	0.830
$\theta_\pi^*$	1.20	4.00	4.00	4.00
$\theta_y^*$	0.33	2.26	2.65	2.67
$\Delta E(\mathcal{W})$	0.00	-40.65	-17.04	-14.90
C.E.	0.00	-1.00	-0.99	-1.00

**Notes:** Optimal parameters of the monetary policy rule for different CBDC designs: col. (1) baseline model (without CBDC); col. (2) CBDC with a fixed interest rate; col. (3) CBDC with a flexible (Taylor rule) interest rate; col. (4) CBDC with a marked-down interest rate. The key parameters optimized are interest rate smoothing ( $\gamma$ ), sensitivity to inflation ( $\theta_\pi$ ) and sensitivity to output ( $\theta_y$ ). Welfare is computed as the stochastic mean of the welfare function  $\mathcal{W}_t = U_t + \beta E_t(\mathcal{W}_{t+1})$  at the second order with pruning.

# Conclusions

- ✓ CBDC amplifies international spillovers of shocks
- ✓ Technical design features matter
  - Capital controls and flexible CBDC interest rate reduce spillovers
  - Quantitative restrictions less effective than interest rate flexibility
- ✓ CBDC increases asymmetries in the international monetary system
- ✓ CBDC reduces monetary policy autonomy in foreign economy (stronger reaction to output and inflation)
- ✓ Extensions:
  - monetary policy shock
  - different preferences;  $\chi_{DC}$ ;  $\xi$
  - zero lower bound
  - optimization of CBDC remuneration rule

Thank you!  
Questions?

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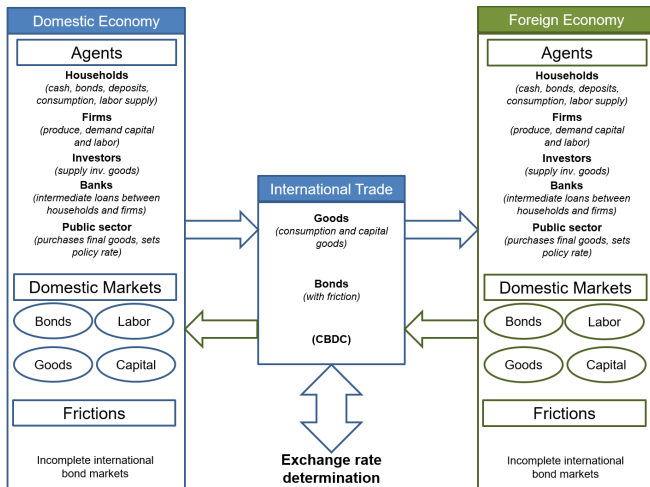
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# Model's chart



## Derivation of key mechanism

Consider the FOCs for bonds and CBDC in the foreign economy:

$$R_t^* = E_t \left( \frac{\lambda_t^*}{\lambda_{t+1}^*} \frac{\pi_{t+1}^*}{\beta^*} \right)$$

$$E_t \left( \frac{\lambda_t^*}{\lambda_{t+1}^*} \frac{\pi_{t+1}^*}{\beta^*} \right) = R_t^{DC} E_t \left( \frac{NER_t}{NER_{t+1}} \right) \left[ 1 + \chi_{DC}^* \frac{\mathcal{G}_{DC,t}^{*'} NER_t}{\lambda_t^*} - \frac{\mathcal{L}_{DC,t}^{*'} NER_t \gamma_t^*}{\lambda_t^*} + \phi^{*,DC} \frac{DC_t^*}{NER_t} \right]^{-1}$$

Equating  $E_t \left( \frac{\lambda_t^*}{\lambda_{t+1}^*} \frac{\pi_{t+1}^*}{\beta^*} \right)$  allows to link the domestic interest rate and the CBDC rate.

# Derivation of key mechanism, con't

$$R_t^* = R_t^{DC} E_t \left( \frac{NER_t}{NER_{t+1}} \right) \left[ 1 + \chi_{DC}^* \frac{\mathcal{G}_{DC,t}^{*'} NER_t}{\lambda_t^*} - \frac{\mathcal{L}_{DC,t}^{*'} NER_t \gamma_t^*}{\lambda_t^*} + \phi^{*,DC} \frac{DC_t^*}{NER_t} \right]^{-1}$$

taking logs:

$$\begin{aligned} \ln R_t^* &= \ln R_t^{DC} + \ln NER_t - E_t(\ln NER_{t+1}) + \\ &\quad - \ln \left[ 1 + \chi_{DC}^* \frac{\mathcal{G}_{DC,t}^{*'} NER_t}{\lambda_t^*} - \frac{\mathcal{L}_{DC,t}^{*'} NER_t \gamma_t^*}{\lambda_t^*} + \phi^{*,DC} \frac{DC_t^*}{NER_t} \right] \end{aligned}$$

and the mark-up  $\mu_t$  is defined as:

$$\left[ 1 + \chi_{DC}^* \frac{\mathcal{G}_{DC,t}^{*'} NER_t}{\lambda_t^*} - \frac{\mathcal{L}_{DC,t}^{*'} NER_t \gamma_t^*}{\lambda_t^*} + \phi^{*,DC} \frac{DC_t^*}{NER_t} \right].$$

## Comparison with standard UIP on bonds

Log-linearized UIP implies (with  $\phi^{*,B} \approx 0$ ):

$$r_t^* - r_t = ner_t - E_t ner_{t+1}$$

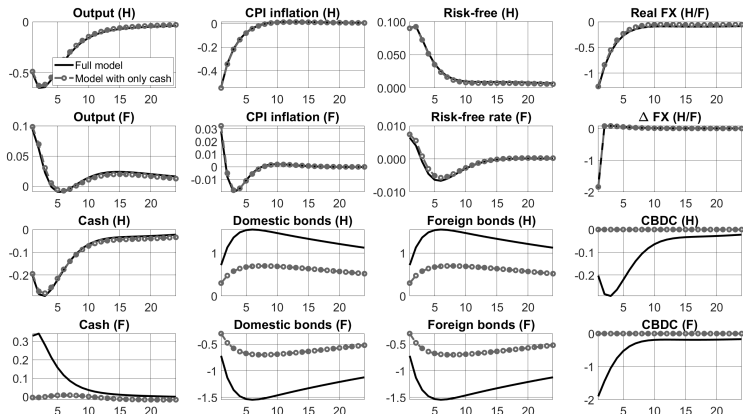
The log-linearized UIP equation for the CBDC is:

$$r_t^* - r_t^{DC} = ner_t - E_t ner_{t+1} + m_t$$

**Notice that:**

- ✓ In standard UIP both  $r_t^*$  and  $r_t$  adjust
- ✓ In CBDC UIP only  $r_t^*$  can adjust
- ✓ In CBDC UIP movements are amplified by the mark-up  $m_t$
- ✓ Spillovers with CBDC are amplified

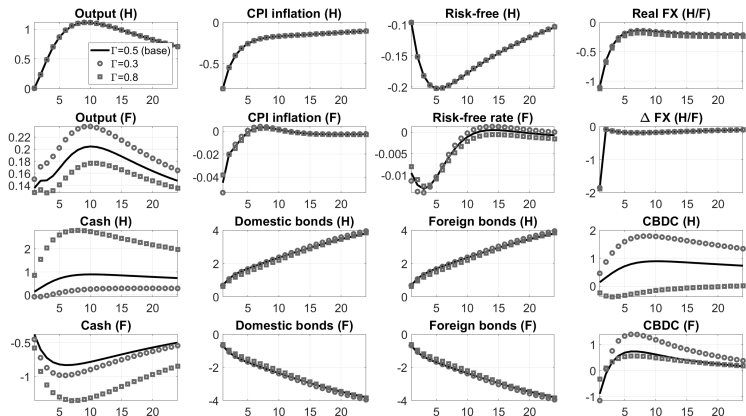
# Monetary policy shock in the domestic economy



**Figure:** Response of selected variables to a one standard deviation contractionary monetary policy shock in the domestic economy.

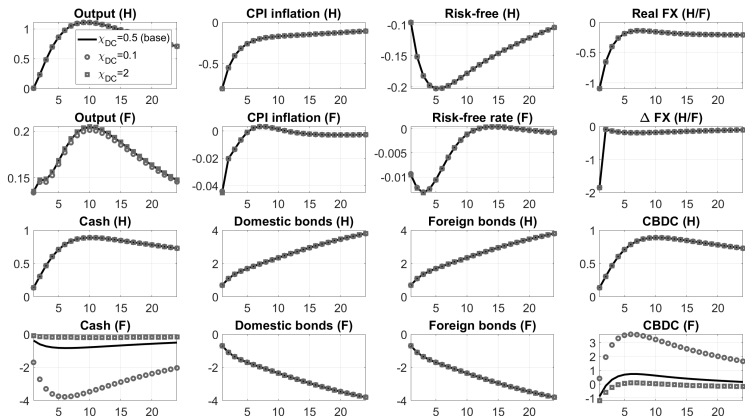
**Notes:** Responses are reported in deviations from the steady state. Solid lines refer to the baseline calibration with a CBDC, dashed lines with circles to simulations without a CBDC. [◀ Go back](#)

# Different preferences for CBDC ( $\Gamma$ )



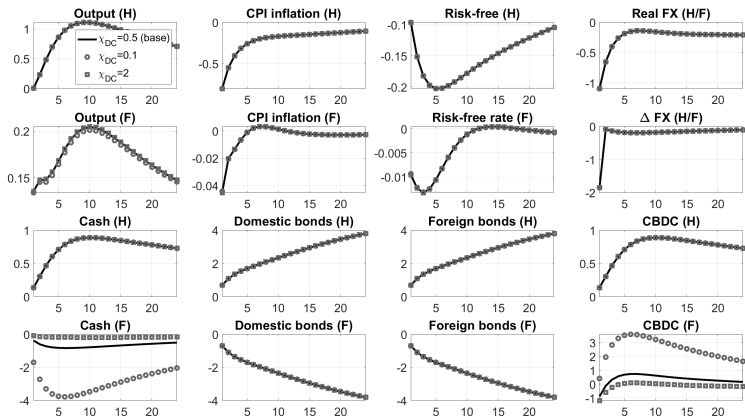
**Figure:** Response of selected variables to a one standard deviation expansionary total factor productivity shock in the domestic economy.

**Notes:** Responses are reported in deviations from the steady state. [◀ Go back](#).

Loading for CBDC in utility ( $\chi_{dc}$ )

**Figure:** Response of selected variables to a one standard deviation expansionary total factor productivity shock in the domestic economy.

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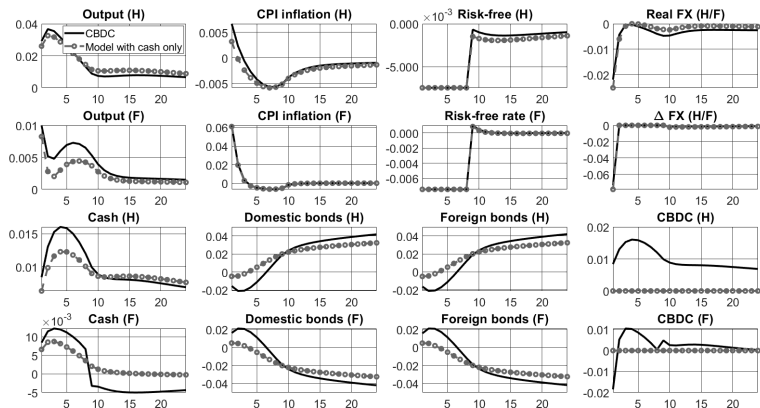
Storage cost for money ( $\zeta$ )

**Figure:** Response of selected variables to a one standard deviation expansionary total factor productivity shock in the domestic economy.

**Notes:** Responses are reported in deviations from the steady state. [◀ Go back](#).



# Simulations at the zero lower bound



**Figure:** Response of selected variables to a 1% expansionary total factor productivity shock in the domestic economy. Solid lines refer to the baseline calibration with a CBDC, dashed lines with circles to a simulation without a CBDC. **Notes:** Responses are reported in deviations from the steady state. The model is simulated assuming that the ZLB binds on impact and then for 2 years. [◀ Go back](#).

# Optimal CBDC remuneration rule

The Taylor rule and the CBDC remuneration rule are:

$$\ln R_t = (1 - \varrho) \ln R_{t-1} + \varrho [R_{ss} + \theta_\pi \ln \pi_t + \theta_y (\ln Y_t - \ln Y_{ss})] + \mathcal{E}_t$$

$$\ln R_t^{DC} = (1 - \varrho_{DC}) \ln R_{t-1}^{DC} + \varrho_{DC} \left[ R_{ss}^{DC} + \theta_\pi^{DC} \ln \pi_t + \theta_y^{DC} (\ln Y_t - \ln Y_{ss}) \right]$$

	$\varrho_{DC}$	$\theta_\pi^{DC}$	$\theta_y^{DC}$	$\theta_Q^{DC}$	$\varrho$	$\theta_\pi$	$\theta_y$
CBDC interest rate rule	0.506	0.230	1.056	0.294			
CBDC and monetary policy rules	0.947	2.714	1.6902	-0.031	0.001	1.561	0.000

**Notes:** Optimal parameters of the CBDC interest-rate rule and the monetary policy rule for the domestic economy. Welfare is computed as the stochastic mean of the welfare function  $\mathcal{W}_t = U_t + \beta E_t(\mathcal{W}_{t+1})$  at the second order with pruning. When the interest rate on CBDC is optimized alone, we keep the parameters of the monetary policy rule at their baseline calibration.

[← Go back](#)