

TIME-VARYING EXCHANGE RATE PASS-THROUGH INTO TERMS OF TRADE

Dr Justas Dainauskas (j.dainauskas@lse.ac.uk)

London School of Economics and Political Science



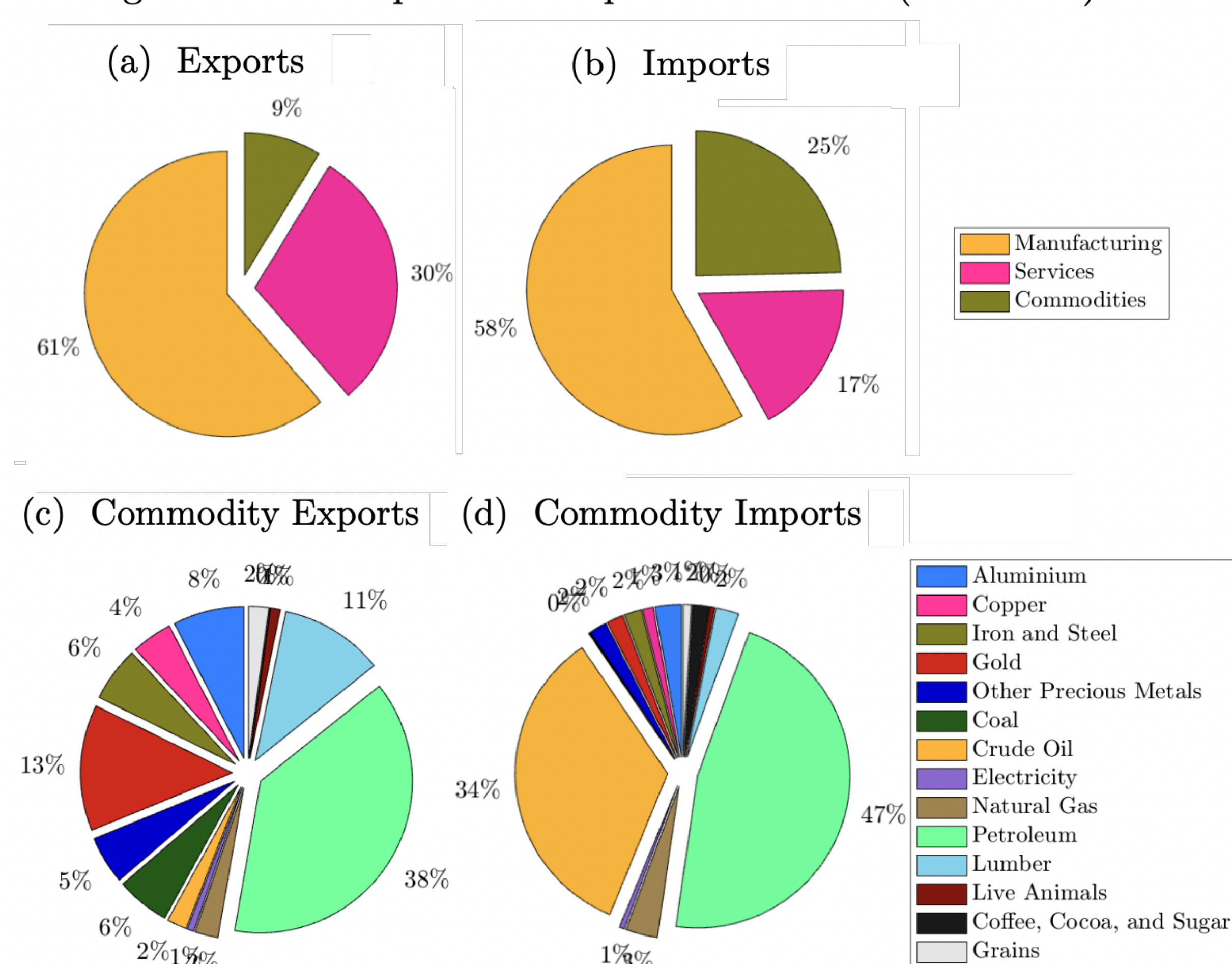
U.S. Dollar: A Dominant Currency

- U.S. pays for 97% of its foreign imports and sells 90% of its exports to the rest of the world using the U.S. dollar ([Gopinath and Rigobon \(2008\)](#))
- This pattern hardly changed throughout 1995-2015 ([Gopinath \(2015\)](#)).
- U.S. dollar also dominates trade invoicing for other countries ([Gopinath et al. \(2020\)](#))
- If U.S. import and export prices are *sticky* in U.S. dollars, then exogenous U.S. dollar depreciations cause the U.S. import (export) prices to increase by 10% (3%).
- U.S. terms of trade, measuring the relative price of imports to exports, would therefore deteriorate by 7%. This magnitude is unusually low.

Is Dollar Invoicing the Same as Dollar Pricing?

- Not all prices are equally sticky.
- [Bils and Klenow \(2004\)](#) show that primary commodity prices adjust far more frequently than non-commodity prices (i.e. manufactured goods and services).
- One quarter and one-tenth of U.S. imports and exports, respectively, are primary commodities (see Figure 1).
- Hypothesis 1: if U.S. terms of trade respond to U.S. dollar depreciations by more than 7%, controlling for confounding factors, then not all prices that are invoiced in U.S. dollars are sticky in U.S. dollars.
- Hypothesis 2: if the amount by which the U.S. terms of trade respond to U.S. dollar depreciations changes over time, controlling for changes in other fundamentals, then price stickiness also changes over time.

Figure 1: U.S. Import and Export Breakdown (1990-2018)



Exchange Rate Pass-Through (ERPT)

- Notation: $\Delta\tau_t = \tau_t - \tau_{t-1}$ and $\Delta e_t = e_t - e_{t-1}$ are the log differences in terms of trade (TOT) and nominal exchange rate (NEER), respectively.
- Definition 1: ERPT measures “how much” and “how fast” Δe_t is transmitted into $\Delta\tau_{t+h}$, where $h = 0, 1, 2, \dots$ is the time horizon.
- Definition 2: transmission of Δe_t into $\Delta\tau_{t+h}$ is said to be: (i) short-run when $h = 0$; (ii) medium-run when $0 < h < \infty$; and (iii) long-run when $h \rightarrow \infty$.
- Standard measurement equation of time-invariant ERPT (e.g. [Campa and Goldberg \(2005\)](#), [Burstein and Gopinath \(2014\)](#)):

$$\Delta\tau_t = \lambda\Delta\tau_{t-1} + \phi\Delta e_t + \mathbf{z}_t\boldsymbol{\zeta} + \varepsilon_t, \quad (1)$$

$-1 \leq \lambda < 1$, $\phi \in [0, 1]$, $\varepsilon_t \sim \text{iid}\mathcal{N}(0, \sigma^2)$, and \mathbf{z}_t is a vector of control variables including the intercept.

- I measure time-varying ERPT using a state-space (SS) model:

$$y_t = \mathbf{x}_t\boldsymbol{\alpha}_t + \varepsilon_t, \quad (2)$$

$$\boldsymbol{\alpha}_t = \boldsymbol{\eta} + \boldsymbol{\gamma}\boldsymbol{\alpha}_{t-1} + \boldsymbol{\delta}\mathbf{s}_t + \mathbf{u}_{t-1}, \quad (3)$$

where $\mathbf{x}_t = [\Delta\tau_{t-1}, \Delta e_t, \mathbf{z}_t]$ is a $1 \times k$ vector of control variables, $\boldsymbol{\alpha}_t = [\lambda_t, \phi_t, \boldsymbol{\zeta}_t']$ is a $k \times 1$ vector of unobservable state variables, and $y_t := \Delta\tau_t$ is a 1×1 measurement variable, $\boldsymbol{\eta} = (\mathbf{I}_k - \boldsymbol{\gamma})\boldsymbol{\alpha}_{0|0}$ is a $k \times 1$ vector of intercepts, $\boldsymbol{\alpha}_{0|0}$ is fixed, $\boldsymbol{\gamma}$ is a diagonal $k \times k$ matrix of autoregressive coefficients, $\boldsymbol{\delta}$ is a $k \times q$ matrix, \mathbf{s}_t is a $q \times 1$ vector of observable factors, such that $k \geq 1$ and $q \geq 1$, $\varepsilon_t \sim \text{iid}\mathcal{N}(0, \sigma^2)$, $\mathbf{u}_t \sim \text{iid}\mathcal{N}(\mathbf{0}_k, \boldsymbol{\Xi})$, $\mathbb{E}[\mathbf{u}_t\varepsilon_t] = \mathbf{0}_k$, $\boldsymbol{\Xi}$ is a diagonal positive-definite $k \times k$ variance-covariance matrix, and $\mathbf{0}_k$ is a $k \times 1$ vector of zeros.

- Because closed-form solution to σ and $\boldsymbol{\Xi}$ does not exist, $\boldsymbol{\alpha}_t$ is estimated using a sequence of four steps: (i) [Kalman \(1960\)](#) filter; (ii) fixed interval Kalman smoother ([de Jong \(1989\)](#)); (iii) quasi maximum likelihood ([Durbin and Koopman \(2012\)](#)); and (iv) parametric bootstrapping ([Rodriguez and Ruiz \(2009\)](#)).

- If Δe_t and ε_t are uncorrelated, ERPT at any time horizon $h = 0, 1, 2, \dots$ is given by

$$\mu_{h,t} = \sum_{i=0}^h \frac{\partial \Delta\tau_{t+i}}{\partial \Delta e_t} = \phi_t \sum_{i=0}^h \lambda_t^i, \quad (4)$$

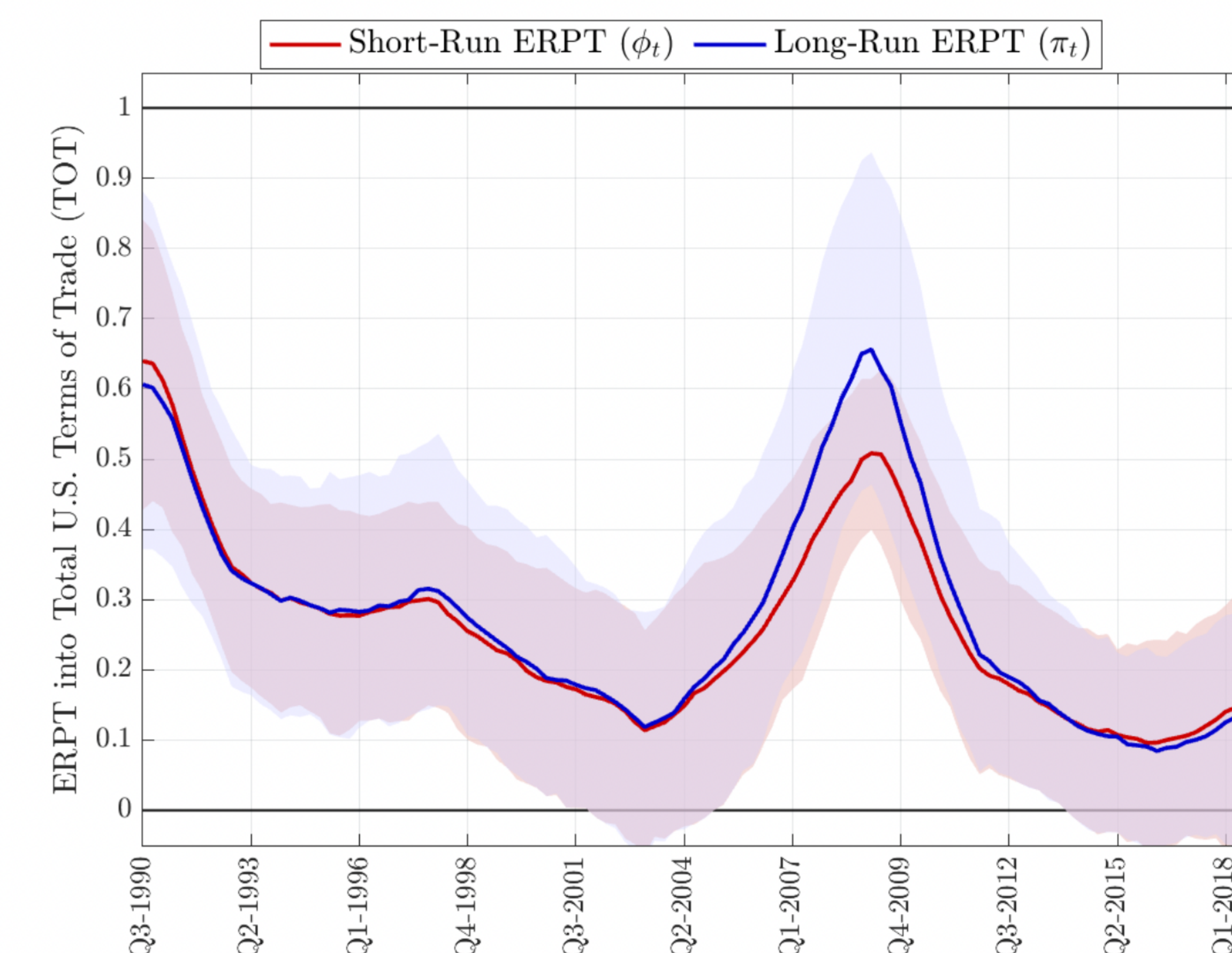
- In the short-run, $\mu_{0,t} := \phi_t$. In the long-run, $\mu_{\infty,t} = \phi_t / (1 - \lambda_t) := \pi_t$.

U.S. Terms of Trade and the U.S. Dollar

- I find a robust time-varying relationship between the U.S. TOT (i.e. incl. commodity and non-commodity prices) and U.S. NEER (see Figure 2).
- By contrast, in the paper, I show that ERPT into TXT (i.e. TOT excl. commodity prices) is virtually constant over time.
- I conclude that ERPT time-variation stems from commodity prices.
- I show that ERPT is counter-cyclical: in 2008-2009 ERPT into TOT peaks at 60-70%, but in 1992-1999 or 2010-2014 it less than 30%.
- Implication: despite being invoiced in U.S. dollars, commodity prices are not always sticky in U.S. dollars, especially not when the U.S. slips into a recession.

- Given the substantial time variation of ERPT into TOT, it can affect the U.S. trade balance adjustments and can be important for FED monetary policy conduct.
- Yet much of the literature is focused on measuring ERPT directly into the U.S. CPI inflation, which tends to be low not only due to U.S. dollar invoicing, but also due to sizeable distribution costs ([Burstein, Neves, and Rebelo \(2003\)](#)).

Figure 2: Time-Varying ERPT into the U.S. Terms of Trade (1990-2018)



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